

# Efficient Bayesian Hierarchical Population Estimation Modelling using INLA-SPDE: Integrating Multiple Data Sources and Spatial Autocorrelation

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## BACKGROUND

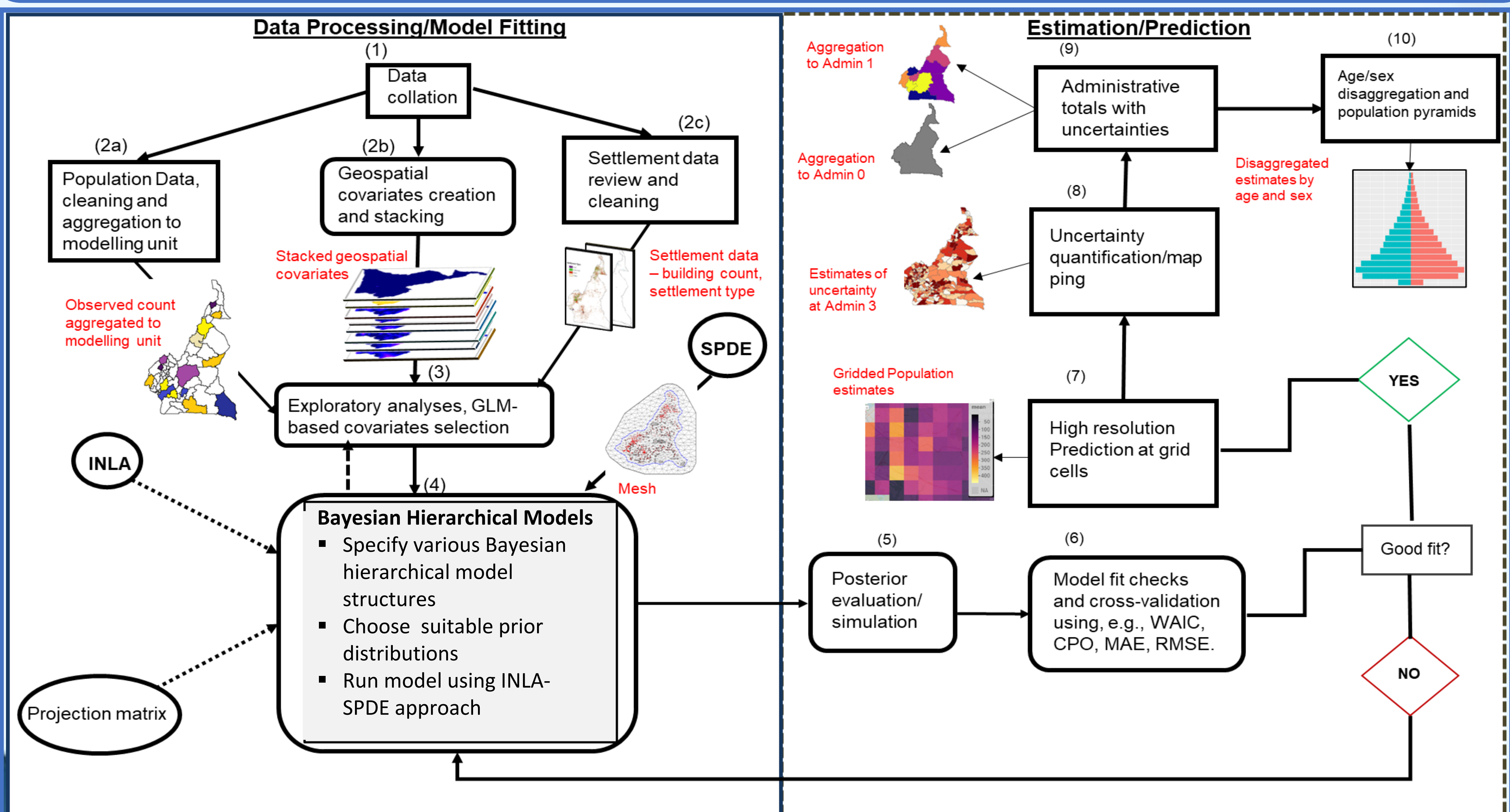
Modelled population estimates provide small area population data that can support governance, equitable resource allocation, and delivery of aid, especially in countries where census data are outdated or incomplete. Bottom-up population modelling approaches [e.g. 1-2] use advanced statistical techniques to combine sample demographic data (counts of people), with geospatial covariates and satellite-derived settlement data, to produce high-resolution population estimates (usually at ~100m regular grid cells). However, while the existing methods have mostly implied spatial dependence of the observations through the geospatial covariates, the latent effects of the potential spatial autocorrelation on the observed data is still not very clear. Here, we produced small area estimates of population in Cameroon (along with uncertainty metrics) using the integrated nested Laplace approximation/stochastic partial differential equation (INLA/SPDE) framework [3], which allowed us to explicitly integrate spatial autocorrelation with five nationally representative household listing datasets within a bottom-up population modelling framework. Our methodology represents an important development within population modelling contexts and has facilitated the development of several other INLA/SPDE-based population modelling techniques developed to address different data challenges across the World.

## DATA:

- **Demographic data:** Five geolocated cluster household listing datasets from nationally-representative household surveys
- **Geospatial covariates:** E.g., Nighttime lights, distance to local roads, distance to market places
- **Settlement data:** Building footprints, settlement type classifications

## METHOD:

- The datasets were collated, processed and cleaned.
- Geospatial covariates were stacked and tested for model fit.
- Spatial autocorrelation was implied through the triangulation of the entire country using non-convex hull mesh.
- Trained model parameters were used to make predictions at 100x100m grid cells.



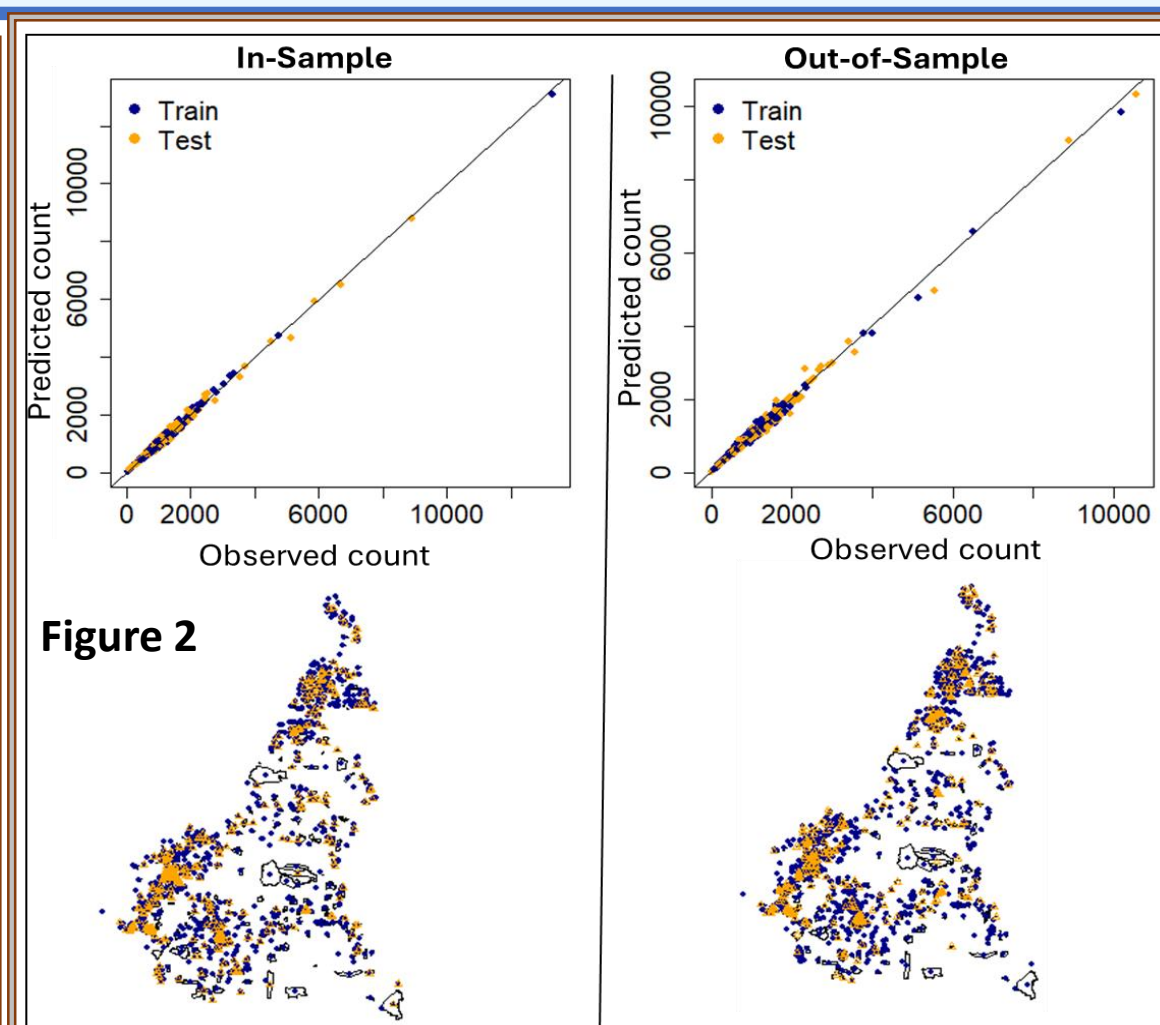
**Figure 1.** Modelling workflow. WAIC – Widely Acceptable Information Criterion; CPO – Conditional Probability Ordinate; MAE – Mean Absolute Error; RMSE – Root Mean Square Error

**Table 1.** Model Cross-Validation

Sample	MAE	RMSE	Absolute BIAS	CORR
In-Sample	58.745	82.527	3.997	0.997
Out-of-sample	63.327	93.278	3.212	0.996

**Table 2.** Estimated total national population

Total	Lower bound	Upper bound
28,663,487	27,147,814	30,612,947



## RESULTS:

- Model cross-validation using both in-sample and out-of-sample cross-validation techniques indicated good predictive ability for the best fit model (Table 1 & Figure 2).
- There is a probability of 95% that the 'true' total national population lies between 27.15M and 30.61M (Table 2)
- The datasets are now published and freely available in the WorldPop data repository



SCAN THE QR CODE TO ACCESS THE POPULATION DATA

## REFERENCES

- [1] Leasure, D. R., W. C. Jochem, E. M. Weber, V. Seaman and A. J. Tatem (2020). "National population mapping from sparse survey data: A hierarchical Bayesian modeling framework to account for uncertainty." *PNAS*: 201913050. DOI: 10.1073/pnas.1913050117. <https://www.pnas.org/doi/pdf/10.1073/pnas.1913050117>
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- [3] Rue, Havard, Sara Martino, and Nicolas Chopin. 2009. "Approximate Bayesian Inference for Latent Gaussian Models by Using Integrated Nested Laplace Approximations." *Journal of the Royal Statistical Society, Series B* 71 (2): 319–92. <https://www.unfpa.org/resources/value-modelled-population-estimates-census-planning-and-preparation>

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